

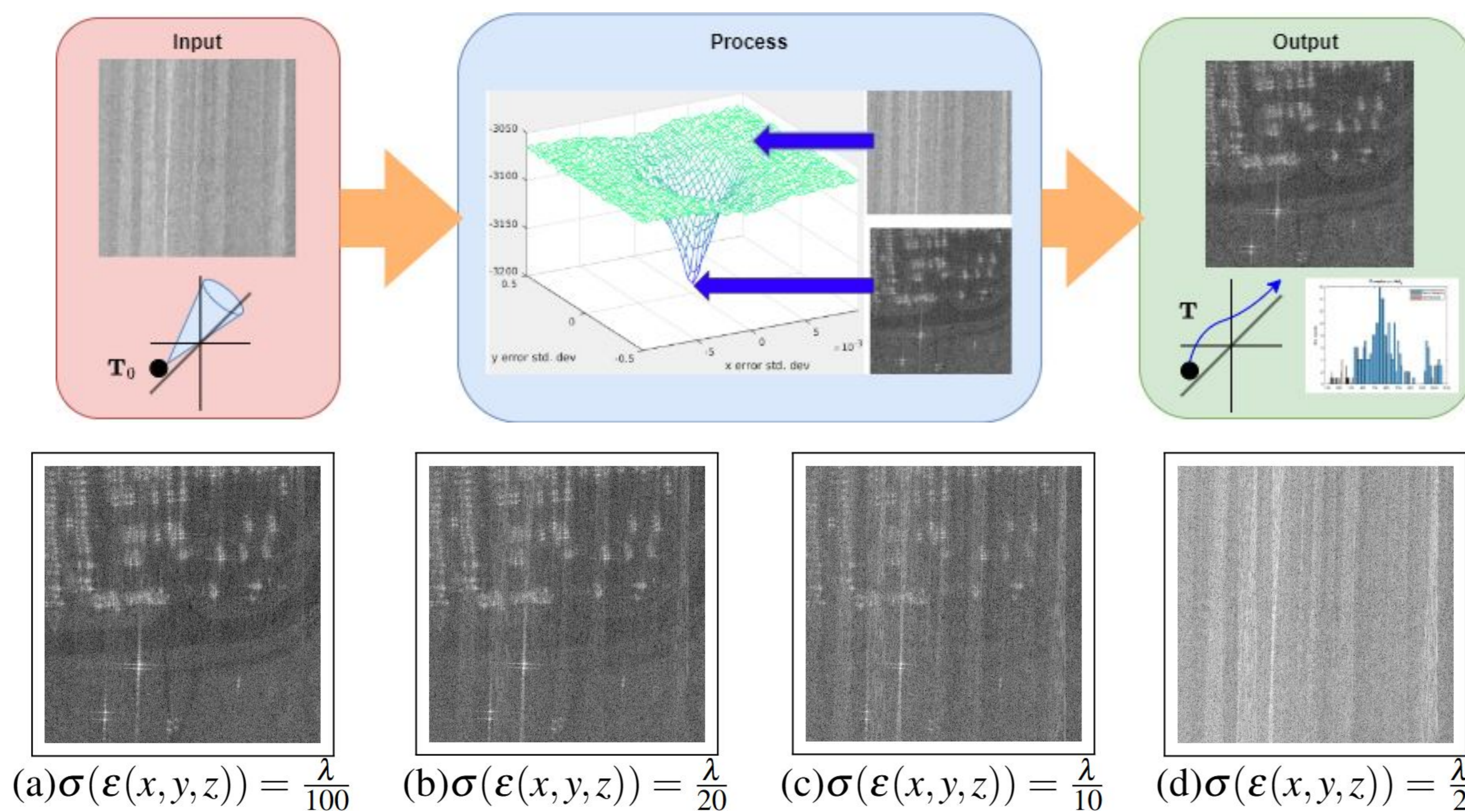
# Deep Learning for GPS-Denied SAR Image Focusing and Vehicle Trajectory Estimation

Chris Beam, Andrew Willis ({cbeam18,arwillis}@charlotte.edu), Kevin Brink (kevin.brink@us.af.mil)

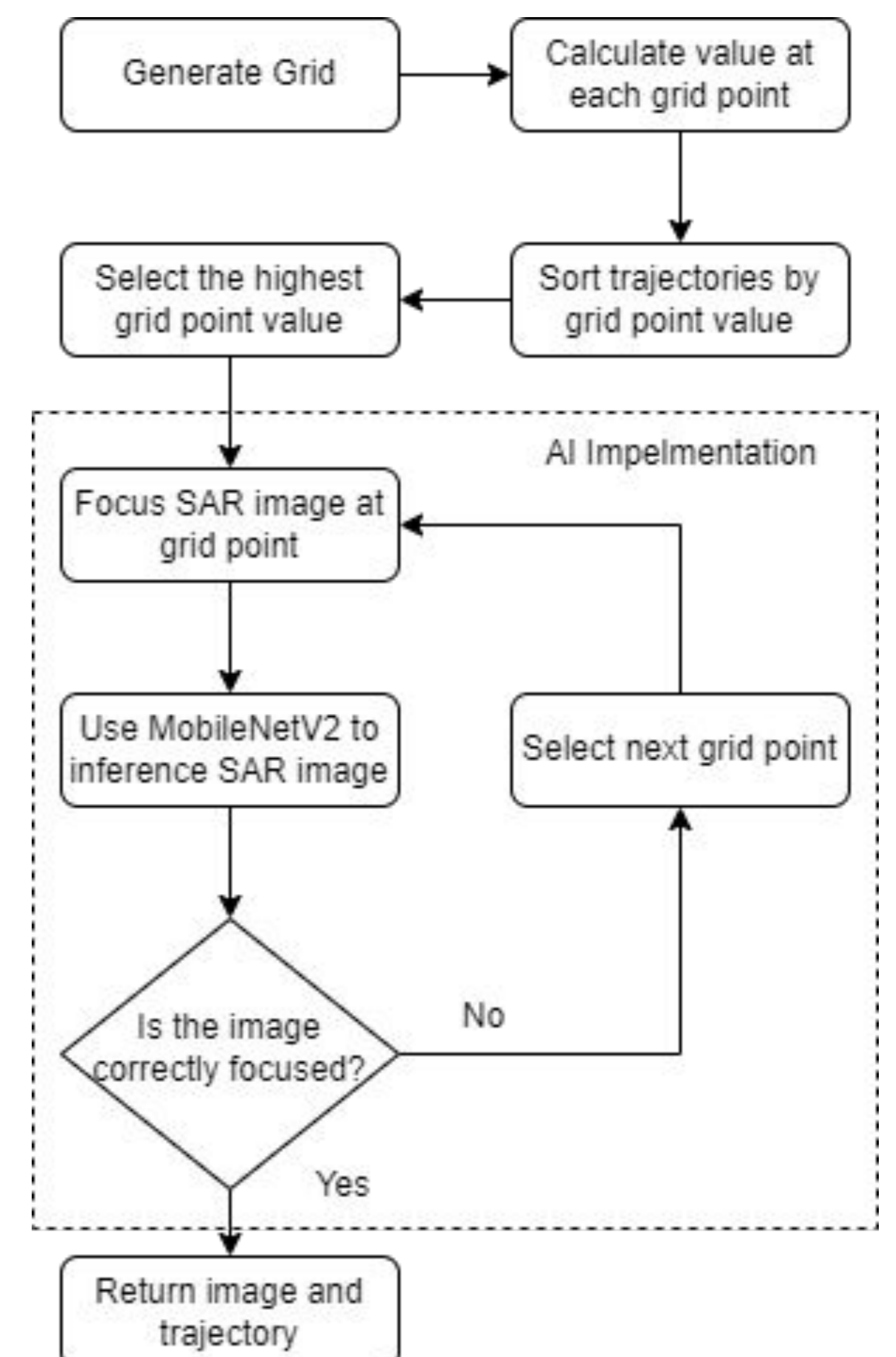
## Overview

Synthetic Aperture Radar (SAR) uses Radio Frequency (RF) radiation pulses to capture backscatter signals from Earth's surface. A major problem with SAR systems is that they are highly sensitive to errors in positioning where focusing fails at position errors above 10% of the wavelength  $\lambda$  [1,2]. This article builds upon prior work described in [3] by:

1. Defining a new performance functional to improve detection of "real-world" and "invalid" SAR images.
2. A new AI approach for classifying "real-world" and "invalid" SAR images.



## Method

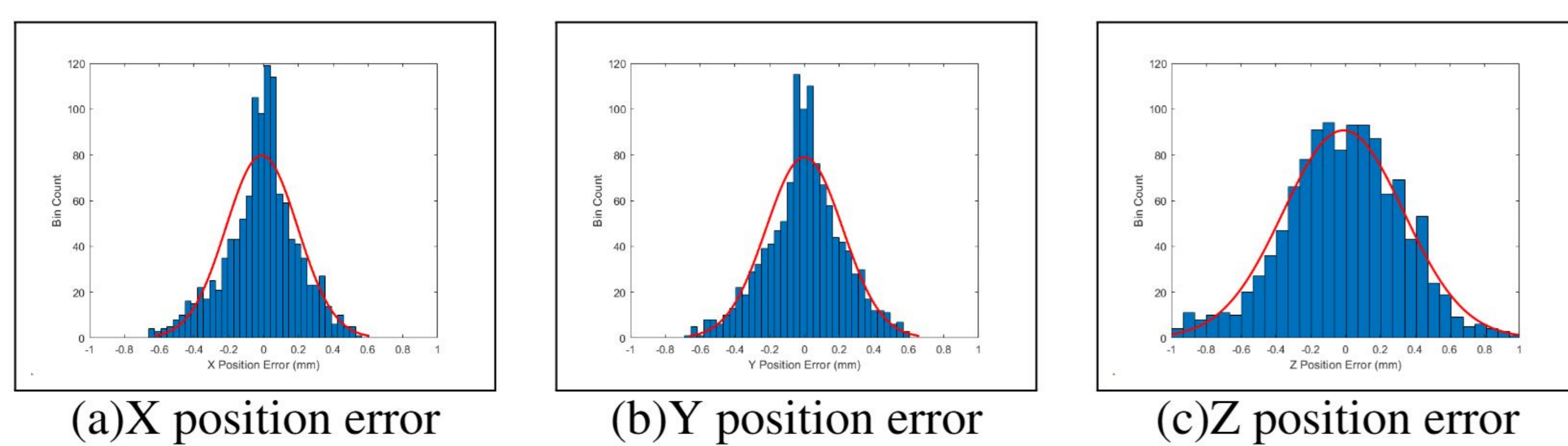


$$\mathbf{F}_D(m, n | \mathbf{T} = \mathbf{T}_i) = \sum_{x=0}^{X-1} \sum_{y=0}^{Y-1} e^{-j2\pi xm/X} e^{-j2\pi yn/Y} \mathbf{I}_D(x, y | \mathbf{T} = \mathbf{T}_i)$$

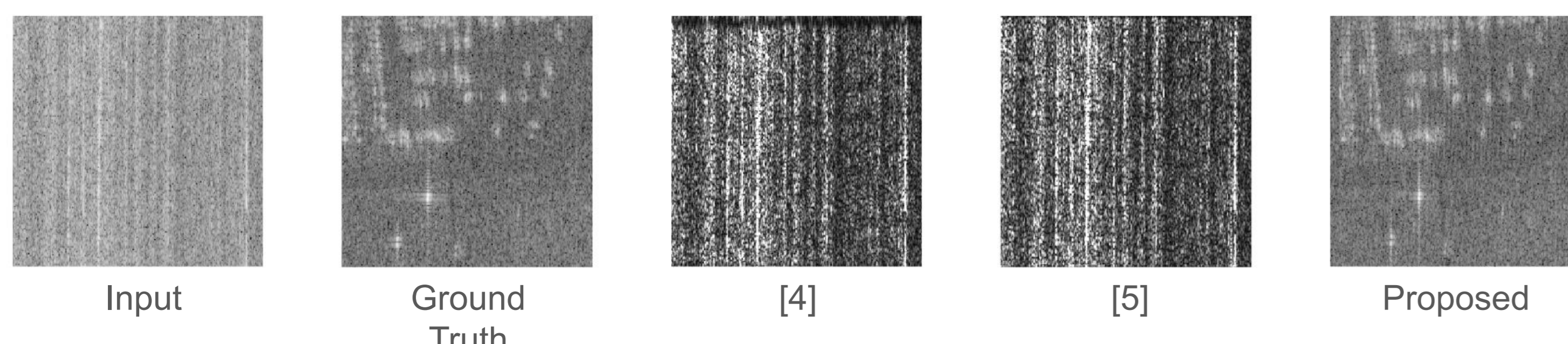
$$\mathbf{Q}(\mathbf{T} = \mathbf{T}_i | \mathcal{D}) = \sum_{m=-M_0}^{M_0} \sum_{n=-N_0}^{N_0} |\mathbf{F}_D(m, n | \mathbf{T} = \mathbf{T}_i)|$$

## Results

- Histogram of trajectory position errors



- Comparison against state-of-the-art autofocus algorithms



- Tables of MobileNetV2 training and trajectory position errors

Input Size	Accuracy	Precision	Recall	AUC
224 <sup>2</sup> x3	0.9962	0.9962	0.9962	1
128 <sup>2</sup> x3	0.9821	0.9821	0.9821	0.986
64 <sup>2</sup> x3	1	1	1	1
32 <sup>2</sup> x3	0.9954	0.9954	0.9954	0.9967
16 <sup>2</sup> x3	0.9996	0.9996	0.9996	1

Table 1: Test dataset metrics for the different MobileNetV2 input sizes.

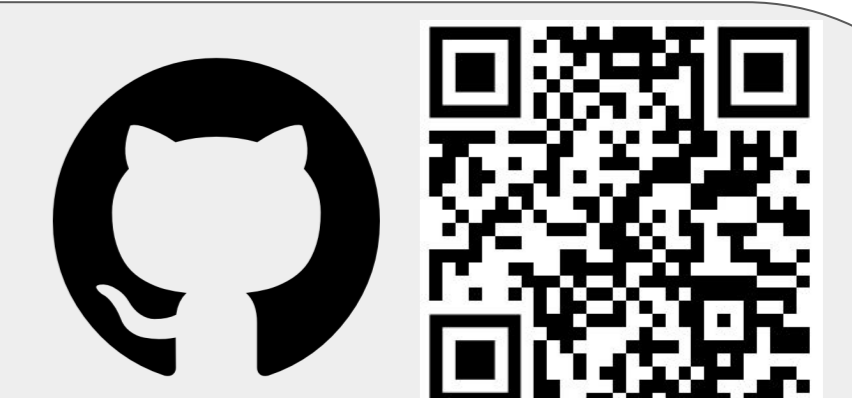
Component	Mean Error (mm)	Std. Dev. Error (mm)
X	-0.0076	0.2402
Y	-0.0044	0.2356
Z	-0.0286	0.3569

Table 2: Error metrics between the relative ground truth trajectory and the estimated trajectory endpoints obtained using our proposed method.

## Conclusion

This article presents a new approach to accurately estimate the trajectory of a radar platform from radar backscatter measurements. This is made possible by two new components: (1) a new performance functional and (2) an AI-based method to identify the correct solutions. MobileNetV2 is used as the CNN model to detect "valid" and "invalid" candidate results. The results show low bias and high accuracy ( $\leq 1$  mm) in trajectory estimates and improved SAR images. Though the estimator is not real-time, it could be deployed to airborne platforms for GNC feedback. The SAR images have potential applications beyond navigational aiding.

## References



- [1] Michael Israel Duersch. Backprojection for Synthetic Aperture Radar. PhD thesis, Brigham Young University, 2013.
- [2] Aaron Evers and Julie Ann Jackson. A comparison of autofocus algorithms for back-projection synthetic aperture radar. In 2020 IEEE International Radar Conference (RADAR). IEEE, apr 2020. doi: 10.1109/radar42522.2020.9114579.
- [3] Andrew Willis, Christopher Beam, Garrett Demeyer, and Kevin Brink. Gpu-accelerated sar image formation in the presence of very large motion error. In IGARSS 2023 - 2023 IEEE International Geoscience and Remote Sensing Symposium, pages 7906–7909, 2023. doi: 10.1109/IGARSS52108.2023.10281891.
- [4] Zhi Liu, Shuyuan Yang, Quanwei Gao, Zhixi Feng, Min Wang, and Licheng Jiao. Afnet and pafnet: Fast and accurate sar autofocus based on deep learning. IEEE Transactions on Geoscience and Remote Sensing, 60:1–13, 2022. doi: 10.1109/TGRS.2022.3217063.
- [5] Zhi Liu, Shuyuan Yang, Zhixi Feng, Quanwei Gao, and Min Wang. Fast sar autofocus based on ensemble convolutional extreme learning machine. Remote Sensing, 13(14):2683, 2021. doi:https://doi.org/10.3390/rs13142683.